



# Designing of Adaptive Hold Logic Using Booth Algorithm

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## ABSTRACT:

Digital multipliers are among the most critical arithmetic functional units. . Therefore, it is important to design reliable high-performance multipliers. In this paper, we propose an aging-aware multiplier design with a novel adaptive hold logic (AHL) circuit. The multiplier is able to provide higher throughput through the variable latency and can adjust the AHL circuit to mitigate performance degradation that is due to the aging effect. Moreover, the proposed architecture can be applied to a column- or row-bypassing multiplier. The experimental results show that our proposed architecture with  $16 \times 16$  and  $32 \times 32$  column-bypassing multipliers can attain up to 62.88% and 76.28% performance improvement, respectively, compared with  $16 \times 16$  and  $32 \times 32$  fixed-latency column-bypassing multipliers.

**Key Terms**— Adaptive hold logic (AHL), negative bias temperature instability (NBTI), positive bias temperature instability (PBTI), reliable multiplier, variable latency.

I. INTRODUCTION DIGITAL multipliers: are among the most critical arithmetic functional units in many applications, such as the Fourier transform, discrete cosine transforms, and digital filtering. The throughput of these applications depends on multipliers, and if the multipliers are too slow, the performance of entire circuits will be reduced. Furthermore,

negative bias temperature instability (NBTI) occurs when a pMOS transistor is under negative bias ( $V_{gs} = -V_{dd}$ ). In this situation, the interaction between inversion layer holes and hydrogen-passivated Si atoms break the Si-H bond generated during the oxidation process, generating H or H<sub>2</sub> molecules. When these molecules diffuse away,

interface traps are left. The accumulated interface traps between silicon and the gate oxide interface result in increased threshold voltage ( $V_{th}$ ), reducing the circuit switching speed. When the biased voltage is removed, the reverse reaction occurs, reducing the NBTI effect. However, the reverse reaction does not eliminate all the interface traps generated during the stress phase, and  $V_{th}$  increased in the long term. Hence, it is important to design a reliable high-performance multiplier. The corresponding effect on an nMOS transistor is positive bias temperature instability (PBTI), which occurs when an nMOS transistor is under positive bias. Compared with the NBTI effect, the PBTI effect is much smaller on oxide/polygate transistors, and therefore is usually ignored. However, for high-k/metal-gate nMOS transistors with significant charge trapping, the PBTI effect can no longer be ignored. In fact, it has been shown that the PBTI effect is more significant than the NBTI effect on 32-nm high-k/metalgate processes. A traditional method to mitigate the aging effect is overdesign [5], [6], including such things as guard-banding and gate oversizing;

however, this approach can be very pessimistic and area and power inefficient. To avoid this problem, many NBTI-aware methodologies have been proposed. An NBTI-aware technology mapping technique was proposed in [7] to guarantee the performance of the circuit during its lifetime. In [8], an NBTI-aware sleep transistor was designed to reduce the aging effects on pMOS sleeptransistors, and the lifetime stability of the power-gated circuits under consideration was improved. Wu and [9] proposed a joint logic restructuring and pin reordering method, which is based on detecting functional symmetries and transistor stacking effects. They also proposed an NBTI optimization method that considered path sensitization dynamic voltage scaling and body-biasing techniques were proposed to reduce power or extend circuit life. These techniques, however, require circuit modification or do not provide optimization of specific circuits. Traditional circuits use critical path delay as the overall circuit clock cycle in order to perform correctly. However, the probability that the critical paths are activated is low. In most cases, the path delay is shorter



than the critical path. For these noncritical paths, using the critical path delay as the overall cycle period will result in significant timing waste. Hence, the variable-latency design was proposed to reduce the timing waste of traditional circuits.

variable-latency design divides the circuit into two parts: 1) shorter paths and 2) longer paths. Shorter paths can execute correctly in one cycle, whereas longer paths need two cycles to execute. When shorter paths are activated frequently, the average latency of variable-latency designs is better than that of traditional designs. For example, several variable-latency adders were proposed using the speculation technique with error detection and recovery. A short path activation function algorithm was proposed in to improve the accuracy of the hold logic and to optimize the performance of the variable-latency circuit. An instruction scheduling algorithm was proposed into schedule the operations on nonuniform latency functional units and improve the performance of Very Long Instruction Word processors. In, a variable-latency pipelined multiplier architecture with a Booth algorithm

was proposed. In, process-variation tolerant architecture for arithmetic units was proposed, where the effect of process-variation is considered to increase the circuit yield. In addition, the critical paths are divided into two shorter paths that could be unequal and the clock cycle is set to the delay of the longer one. These research designs were able to reduce the timing waste of traditional circuits to improve performance, but they did not consider the aging effect and could not adjust themselves during the runtime. A variable-latency adder design that considers the aging effect was proposed in and. However, no variable-latency multiplier design that considers the aging effect and can adjust dynamically has been done. A. Paper Contribution In this paper, we propose an aging-aware reliable multiplier design with a novel adaptive hold logic (AHL) circuit. The multiplier is based on the variable-latency technique and can adjust the AHL circuit to achieve reliable operation under the influence of NBTI and PBTI effects. To be specific, the contributions of this paper are summarized as follows: 1) novel variable-latency multiplier architecture with an AHL circuit. The

AHL circuit can decide whether the input patterns require one or two cycles and can adjust the judging criteria to ensure that there is minimum performance degradation after considerable aging occurs; 2) comprehensive analysis and comparison of the multiplier's performance under different cycle periods to show the effectiveness of our proposed architecture; 3) an aging-aware reliable multiplier design method that is suitable for large multipliers. Although the experiment is performed in 16- and 32-bit multipliers, our proposed architecture can be easily extended to large designs;

### 1.1 AHL features.

In this paper, we propose an aging-aware reliable multiplier design with a novel adaptive hold logic (AHL) circuit. The multiplier is based on the variable-latency technique and can adjust the AHL circuit to achieve reliable operation under the influence of NBTI and PBTI effects. To be specific, the contributions of this paper are summarized as follows:

1) novel variable-latency multiplier architecture with an

AHL circuit. The AHL circuit can decide whether the input patterns require one or two cycles and can adjust the judging criteria to ensure that there is minimum performance degradation after considerable aging occurs;

2) comprehensive analysis and comparison of the multiplier's performance under different cycle periods to show the effectiveness of our proposed architecture;

3) an aging-aware reliable multiplier design method that is suitable for large multipliers. Although the experiment is performed in 16- and 32-bit multipliers, our proposed architecture can be easily extended to large designs;

4) the experimental results show that our proposed architecture with the  $16 \times 16$  and  $32 \times 32$  column-bypassing multipliers can attain up to 62.88% and 76.28% performance improvement compared with the  $16 \times 16$  and  $32 \times 32$  fixed-latency column-bypassing (FLCB) multipliers. In addition, our proposed architecture with  $16 \times 16$  and  $32 \times 32$  row-bypassing multipliers can achieve up to 80.17% and 69.40%

performance improvement as compared with  $16 \times 16$  and  $32 \times 32$  fixed-latency row-bypassing multipliers.

The paper is organized as follows. Section II introduces the background of the column-bypassing multiplier, row-bypassing multiplier, variable-latency design, and NBTI/PBTI models. Section III details the aging-aware variable-latency multiplier based on the column- or rowbypassing multiplier. The experimental setup and results are presented in Section IV. Section V concludes this paper.

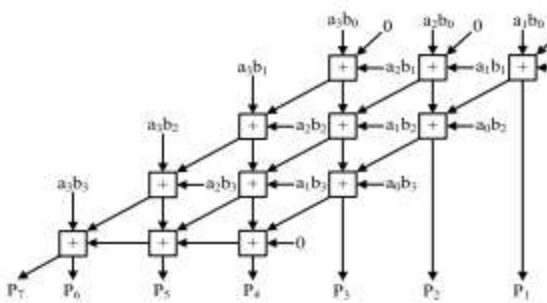


Fig. 1.  $4 \times 4$  normal AM.

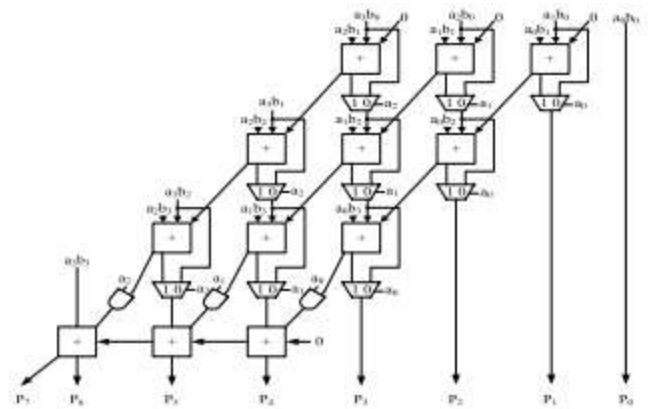


Fig. 2.  $4 \times 4$  column-bypassing multiplier

## EXISTING METHOD

Multiplication is one of the complex arithmetic operations [6]. In most of the signal processing algorithms multiplication is a root operation whereas multipliers have large area, consume considerable power and long latency. So, in low-power VLSI system design, low-power multiplier design is also an important part.

Mostly architecture of parallel multipliers can be classified into three parts: bit generation of primary partial product by using simple AND gates or by using any recoding strategies; bit compression of partial product by using any irregular array of logarithmic tree or by using a regular array; and the final addition [6].

The main part of this paper is the reduction tree technique which is used for designing a new Baugh Wooley multiplier architecture. High Performance Multiplier (HPM) reduction tree [6], [8] is based mainly on the generated partial product compression [1]. It is completely regular and the connectivity of the adding cells in HPM is in the triangular shape. The reason for using triangular shaped is that the triangular cell placement in the reduction tree technique has a shorter wire length [8].

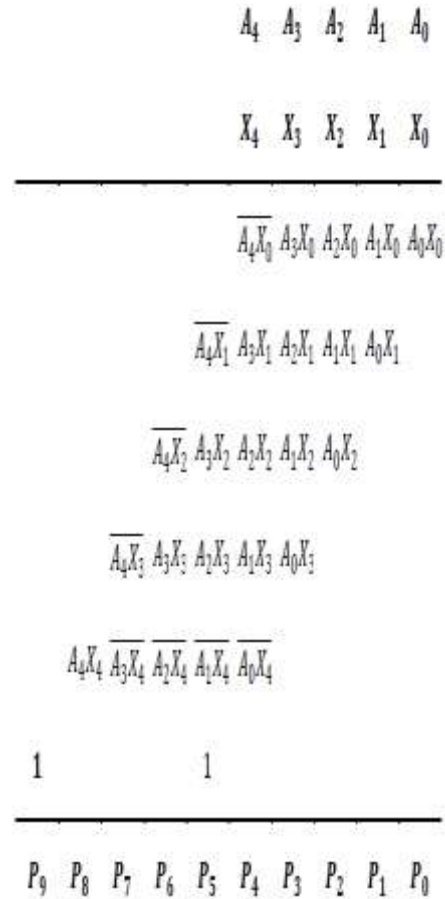


Fig-1: Illustration of 5 bit Baugh Wooley Multiplier Algorithm.

## 2. BAUGH WOOLEY MULTIPLIER

The Baugh-Wooley multiplication is one of the efficient methods to handle the sign bits. This approach has been developed in order to design regular multipliers, suited for 2's complement numbers [2]. Let

two n-bit numbers, multiplier (A) and multiplicand (B), to be multiplied. A and B can be represented as

$$A = -a_{n-1}2^{n-1} + \sum_{i=0}^{n-2} a_i 2^i \quad (1)$$

$$B = -b_{n-1}2^{n-1} + \sum_{i=0}^{n-2} b_i 2^i \quad (2)$$

Where the ai's and bi's are the bits in A and B, respectively, and an-1 and bn-1 are the sign bits. The product, P = A x B, is given

$$P = A \times B = \left( -a_{n-1}2^{n-1} + \sum_{i=0}^{n-2} a_i 2^i \right) \times \left( -b_{n-1}2^{n-1} + \sum_{i=0}^{n-2} b_i 2^i \right)$$

$$= a_{n-1}b_{n-1}2^{2n-2} + \sum_{i=0}^{n-2} a_i 2^i \sum_{j=0}^{n-2} b_j 2^j - 2^{n-1} \sum_{i=0}^{n-2} a_i b_{n-1} 2^i - 2^{n-1} \sum_{j=0}^{n-2} a_{n-1} b_j 2^j \quad (3)$$

by the equation:

The final product can be generated by subtracting the last two positive terms from the first two terms [2].

Instead of doing subtraction operation, it is possible to obtain the 2's complement of the last two terms and add all terms to get the final product.

The last two terms are n-1 bits in which each that extend in binary weight from position 2n-1 up to 22n-3. On the other hand, the final product is 2n bits and extends in binary weight from 20 up to 22n-1. At first pad each of the last two terms in the product P equation with zeros to obtain a 2n-bit number to be able to add it with the other terms. Then the padded terms extend in binary weight from 20 up to 22n-1 [3]. Let X is one of the last two terms that can represent it with zero padding as

$$X = -0 \times 2^{2n-1} + 0 \times 2^{2n-2} + 2^{n-1} \sum_{i=0}^{n-2} x_i 2^i + \sum_{j=0}^{n-2} x_j 2^j \quad (4)$$

The final product [3],  $P = A \times B$  becomes:

$$\begin{aligned} P &= A \times B \\ &= a_{n-1}b_{n-1}2^{2n-2} + \sum_{i=0}^{n-2} a_i 2^i \sum_{j=0}^{n-2} b_j 2^j \\ &+ 2^{n-1} \sum_{i=0}^{n-2} a_i b_{n-1} 2^i + 2^{n-1} \sum_{j=0}^{n-2} a_{n-1} b_j 2^j \\ &\quad - 2^{2n-1} + 2^n \quad (5) \end{aligned}$$

Let A and B are 4-bit binary numbers, then the product [3],  $P = A \times B$  will be 8 bit long and is

$$\begin{aligned} P &= a_3 b_3 2^6 + \sum_{i=0}^2 a_i 2^i \sum_{j=0}^2 b_j 2^j \\ &+ 2^3 \sum_{i=0}^2 a_i b_3 2^i + 2^3 \sum_{j=0}^2 a_3 b_j 2^j \\ &\quad - 2^7 + 2^4 \quad (6) \end{aligned}$$

The block diagram for 4 bit Baugh Wooley multiplier is shown in Fig 3 and the detailed structure of each block has been shown in Fig 4.

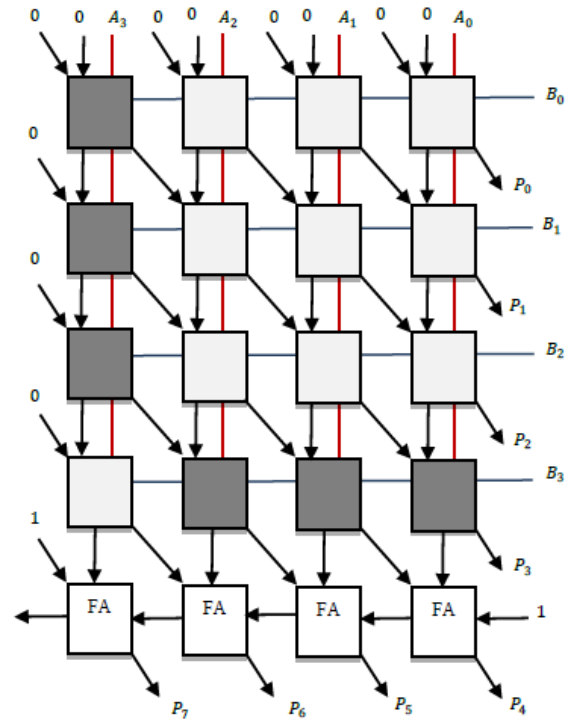


Fig-3: Block diagram of 4 bit Baugh Wooley

## PROPOSED AGING-AWARE MULTIPLIER

This section details the proposed aging-aware reliable multiplier design. It introduces the overall architecture and the functions of each component and also describes how to design AHL that adjusts the circuit when significant aging occurs.

### 1 PROPOSED ARCHITECTURE





Fig. 11. Razor flip flops

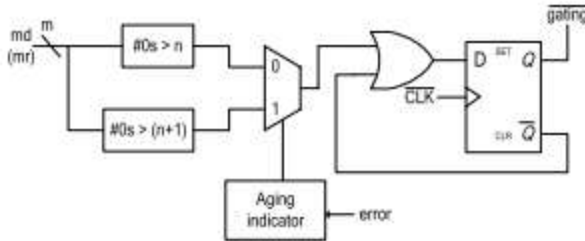


Fig. 12. Diagram of AHL (md means multiplicand; mr means multiplier)

Fig. 11 shows the details of Razor flip-flops. A 1-bit Razor flip-flop contains a main flip-flop, shadow latch, XOR gate, and mux. The main flip-flop catches the execution result for the combination circuit using a normal clock signal, and the shadow latch catches the execution result using a delayed clock signal, which is slower than the normal clock signal. If the latched bit of the shadow latch is different from that of the main flip-flop, this means the path delay of the current operation exceeds the cycle period, and the main flip-flop catches an incorrect result. If errors occur, the Razor flip-flop will set the error signal to 1 to notify the system to reexecute the operation and notify the AHL circuit that an error has occurred. We use Razor flip-flops to detect whether an operation that is considered to be a one-cycle pattern

can really finish in a cycle. If not, the operation is reexecuted with two cycles. Although the reexecution may seem costly, the overall cost is low because the reexecution frequency is low. More details for the Razor flip-flop can be found in [27].

The AHL circuit is the key component in the aging-ware variable-latency multiplier. Fig. 12 shows the details of the AHL circuit. The AHL circuit contains an aging indicator, two judging blocks, one mux, and one D flip-flop. The aging indicator indicates whether the circuit has suffered significant performance degradation due to the aging effect. The aging indicator is implemented in a simple counter that counts the number of errors over a certain amount of operations and is reset to zero at the end of those operations. If the cycle period is too short, the column- or row-bypassing multiplier is not able to complete these operations successfully, causing timing violations. These timing violations will be caught by the Razor flip-flops, which generate error signals. If errors happen frequently and exceed a predefined threshold, it means the circuit has suffered

significant timing degradation due to the aging effect, and the aging indicator will output signal 1; otherwise, it will output 0 to indicate the aging effect is still not significant, and no actions are needed.

The first judging block in the AHL circuit will output 1 if the number of zeros in the multiplicand (multiplier for the row-bypassing multiplier) is larger than  $n$  ( $n$  is a positive number, which will be discussed in Section IV), and the second judging block in the AHL circuit will output 1 if the number of zeros in the multiplicand (multiplier) is larger than  $n + 1$ . They are both employed to decide whether an input pattern requires one or two cycles, but only one of them will be chosen at a time. In the beginning, the aging effect is not significant, and the aging indicator produces 0, so the first judging block is used. After a period of time when the aging effect becomes significant, the second judging block is chosen. Compared with the first judging block, the second judging block allows a smaller number of patterns to become one-cycle patterns because it

requires more zeros in the multiplicand (multiplier)

The details of the operation of the AHL circuit are as follows: when an input pattern arrives, both judging blocks will decide whether the pattern requires one cycle or two cycles to complete and pass both results to the multiplexer. The multiplexer selects one of either result based on the output of the aging indicator. Then an OR operation is performed between the result of the multiplexer, and the  $Q^-$  signal is used to determine the input of the D flip-flop. When the pattern requires one cycle, the output of the multiplexer is 1. The  $\text{!(gating)}$  signal will become 1, and the input flip flops will latch new data in the next cycle. On the other hand, when the output of the multiplexer is 0, which means the input pattern requires two cycles to complete, the OR gate will output 0 to the D flip-flop. Therefore, the  $\text{!(gating)}$  signal will be 0 to disable the clock signal of the input flip-flops in the next cycle. Note that only a cycle of the input flip-flop will be disabled because the D flip-flop will latch 1 in the next cycle.

The overall flow of our proposed architecture is as follows: when input patterns arrive, the column- or row-bypassing multiplier, and the AHL circuit execute simultaneously. According to the number of zeros in the multiplicand (multiplier), the AHL circuit decides if the input patterns require one or two cycles. If the input pattern requires two cycles to complete, the AHL will output 0 to disable the clock signal of the flip-flops. Otherwise, the AHL will output 1 for normal operations. When the column- or row-bypassing multiplier finishes the operation, the result will be passed to the Razor flip-flops. The Razor flip-flops check whether there is the path delay timing violation. If timing violations occur, it means the cycle period is not long enough for the current operation to complete and that the execution result of the multiplier is incorrect. Thus, the Razor flip-flops will output an error to inform the system that the current operation needs to be reexecuted using two cycles to ensure the operation is correct. In this situation, the extra reexecution cycles caused by timing violation incurs a penalty to overall average latency. However, our proposed AHL circuit can accurately

predict whether the input patterns require one or two cycles in most cases. Only a few input patterns may cause a timing variation when the AHL circuit judges incorrectly. In this case, the extra reexecution cycles did not produce significant timing degradation.

In summary, our proposed multiplier design has three key features. First, it is a variable-latency design that minimizes the timing waste of the noncritical paths. Second, it can provide reliable operations even after the aging effect occurs. The Razor flip-flops detect the timing violations and reexecute the operations using two cycles. Finally, our architecture can adjust the percentage of one-cycle patterns to minimize performance degradation due to the aging effect. When the circuit is aged, and many errors occur, the AHL circuit uses the second judging block to decide if an input is one cycle or two cycles.

Timing Summary:

Speed Grade: -5

Minimum period: 6.819ns (Maximum Frequency: 146.646MHz)  
Minimum input arrival time before clock: 72.483ns  
Maximum output required time after clock: 4.063ns  
Maximum combinational path delay: No path found

	Total	Dynamic	Quiescent
Supply Power (W)	0.081	0.000	0.081

Device Utilization Summary				
Logic Utilization	Used	Available	Utilization	Note(s)
Number of Slice Flip Flops	1,09	9,312	1%	
Number of 4 input LUTs	3,262	9,312	35%	
Number of occupied Slices	1,885	4,800	39%	
Number of Slices containing only related logic	1,885	1,885	100%	
Number of Slices containing unrelated logic	0	1,885	0%	
Total Number of 4 input LUTs	3,262	9,312	35%	
Number of bonded I/Os	130	333	39%	
Number of BRAMs	1	24	4%	
Average Percent of Non-Clock Ports	3.3%			

## Conclusion:

This paper proposed an aging-aware variable-latency multiplier design with the AHL. The multiplier is able to adjust the AHL to mitigate performance degradation due to increased delay. The experimental results show that our proposed architecture with  $16 \times 16$  and  $32 \times 32$  column-bypassing multipliers can attain up to 62.88% and 76.28% performance improvement compared with the  $16 \times 16$  and  $32 \times 32$  FLCB multipliers, respectively. Furthermore, our proposed architecture with the  $16 \times 16$  and  $32 \times 32$  row-bypassing multipliers can achieve up to 80.17% and 69.40% performance improvement compared with the  $16 \times 16$  and  $32 \times 32$  FLRB multipliers.

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