

Kinematic Design And Analysis Of Six Degrees Of Freedom Manipulator

Y.SHIVA¹, Dr. G. SATISH BABU²

Research scholar¹

Professor, Department of Mechanical Engineering²

JNTUHCEH, Hyderabad.

Abstract:

Mechanical technology has been a moving subject for educators to instruct and for understudies to learn. One of the significant viewpoints that make it troublesome is the restricted capacity to see and imagine the ideas suitably at the hour of educating. The majority of the modern robots are depicted geometrically by their Denavit-Hartenberg (DH) parameters, which are additionally hard to see for understudies. Understudies will locate the subject simpler to learn in the event that they can imagine in 3 measurements. Apparatuses that guide its learning have been created by colleges over the world as alluded somewhere else. This paper proposes RoboAnalyzer, a 3D model based programming that can be utilized to instruct mechanical autonomy subjects to undergrad and postgraduate courses in building schools in India and somewhere else. In the present implementation, it tends to be utilized to learn DH parameters, forward kinematics of sequential robots with revolute joints and permits 3D movement and diagram plots as yield.

Keywords: Kinematic Design, six degree of freedom, Robots, 3D model based programming.

1. Introduction

Mechanical technology is a field identified with the structure, improvement, control and use of robots in industry, training, inquires about, stimulation, restorative applications and so on. It has been advancing at a quicker rate and subsequently it discovers its place in the educational plan of the colleges and is in extraordinary interest.

Apply autonomy course for mechanical building streams generally incorporates the hypothesis of the plan and working of a robot as drawings, pictures of robots and reasonable robots in real life. In spite of the fact that the initial two are simpler to accomplish by numerous colleges, the last can be accomplished by a not many which approach indus-preliminary robots. Without seeing a genuine robot it is hard to fathom its movement in three-dimensional Cartesian space. Consequently, there exists an extraordinary interest for instructing helps that help understudies to imagine a robots development as 3D movements.

2. Kinematics and Jacobian Matrix Modelling

In this area, the forward and opposite kinematics models of the 6R decoupled controller are worked by D-H technique and

diagnostic strategy [Chapelle, 2004, González-Palacios, 2013]. At that point the Jacobian grid is inferred by differential change technique. The D-H arrange frameworks of the 6R decoupled controller are appeared in Figure 1 and the relating D-H parameters are appeared in Table 1. The controller's last three back to back joint tomahawks cross at a typical point — fulfilling the Pieper criterion. itude edges of the controller end-effector in X-Y-Z fixed edges organize framework are as following, where are alluded to as move, pitch, yaw edges, separately.

2. Kinematics and Jacobian Matrix Modeling In this area, the forward and opposite kinematics models of the 6R decoupled controller are worked by D-H technique and diagnostic strategy [Chapelle, 2004, González-Palacios, 2013]. At that point the Jacobian grid is inferred by differential change technique.

$$x=l_1\cos\theta_1+l_2\cos(\theta_1+\theta_2)+l_3\cos(\theta_1+\theta_2+\theta_3) \dots(1)$$

$$y=l_1\sin\theta_1+l_2\sin(\theta_1+\theta_2)+l_3\sin(\theta_1+\theta_2+\theta_3) \dots(2)$$

$$\phi=(\theta_1+\theta_2+\theta_3)P_2 = a_3 \cdot S_{23} - a_2 \cdot S_2 \dots(3)$$

Thus, from eqs.(35) and (36) we find:

$$a_3 \cdot C_{23} = P_1 - a_2 \cdot C_2 \dots(4)$$

$$a_3 \cdot S_{23} = P_2 - a_2 \cdot S_2 \dots(5)$$

Hence from Eqs(37) and (38) we have:

$$^2A_3 = (P_1 - a_2 \cdot c_2) + (P_2 - a_2 \cdot S_2) \dots(6)$$

Which yield the following:

$$a_3 \cdot C_{23} = P_1 - a_2 \cdot C_2 \dots(7)$$

$$a_3 \cdot S_{23} = P_2 - a_2 \cdot S_2 \dots(8)$$

Then it clearly follows that:

2.1 Forward Kinematics

The D-H arrange frameworks of the 6R decoupled controller are appeared in Figure 1 and the relating D-H parameters are appeared in Table 1. The controller's last three back to back joint

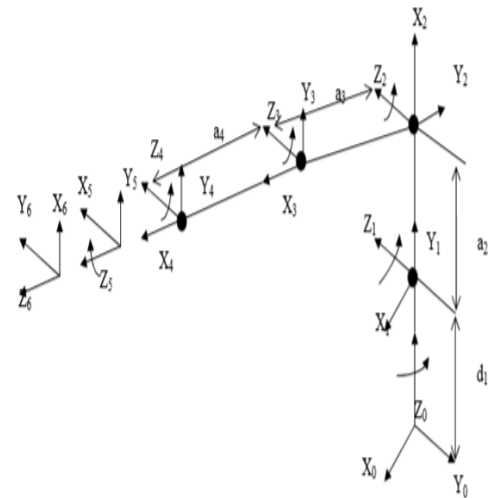


Fig-2: Link frame assignment for MA-2000 Robot with first version of gripper.

Joint	θ_i	α_i	a_i	d_i
1	θ_1	90	0	d_1
2	θ_2	0	a_2	0
3	θ_3	0	a_3	0
4	θ_4	90	a_4	0
5	θ_5	90	0	0
6	θ_6	0	0	d_6

Table-1: joint parameter for 6-DOF robot with first version

$${}^0T_1 = \begin{bmatrix} C_1 & 0 & S_1 & 0 \\ S_1 & 0 & -C_1 & 0 \\ 0 & 1 & 0 & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \dots(8)$$

$${}^1T_2 = \begin{bmatrix} C_2 & -S_2 & 0 & a_2C_2 \\ S_2 & C_2 & 0 & a_2S_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \dots(9)$$

$${}^2T_3 = \begin{bmatrix} C_3 & -S_3 & 0 & a_3C_3 \\ S_3 & C_3 & 0 & a_3S_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \dots(10)$$

$${}^3T_4 = \begin{bmatrix} C_4 & 0 & S_4 & a_4C_4 \\ S_4 & 0 & -C_4 & a_4S_4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \dots(11)$$

$${}^4T_5 = \begin{bmatrix} C_5 & 0 & S_5 & 0 \\ S_5 & 0 & -C_5 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \dots(12)$$

$${}^5T_6 = \begin{bmatrix} C_6 & -S_6 & 0 & 0 \\ S_6 & C_6 & 0 & 0 \\ 0 & 0 & 1 & d_6 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

tomahawks cross at a typical.

Increasing the networks T1 through T6 and setting the outcome equivalent 0. T yields the accompanying twelve conditions for the assurance to 6 the vector of the joint point

$$n_x = s_1.(c_4s_6 + s_4c_5c_6) - c_1.[c_6s_{23}s_5 + c_{23}.(s_4s_6 - c_4c_5c_6)]; \dots(14)$$

$$n_y = s_1.(c_4c_6 - s_4c_5s_6) + c_1[s_{23}s_5s_6 - c_{23}(s_4c_6 + c_4c_5s_6)]; \dots(15)$$

$$n_z = -s_1s_4s_5 - c_1.(s_{23}c_5 + c_{23}c_4s_5); \dots(16)$$

$$O_x = s_1.[c_{23}(c_4c_5c_6 - s_4s_6) - s_{23}s_5c_6] - c_1.(c_4s_6 + s_4c_5c_6); \dots(17)$$

$$O_y = s_1.[c_2.(c_4c_5c_6 - s_4s_6) - s_{23}.s_5c_6] - c_1.(c_4s_6 + s_4c_5c_6); \dots(18)$$

$$O_z = s_1.(s_{23}.c_5 + c_{23}.c_4s_5) + c_1s_4s_5; \dots(19)$$

$$a_x = s_{23}.(s_4s_6 - c_4c_5c_6) - c_{23}s_5c_6; \dots(20)$$

$$a_y = s_{23}.(s_4c_6 + c_4c_5s_6) + c_{23}s_5s_6; \dots(21)$$

$$a_z = s_{23}.c_4s_5 - c_{23}c_5; \dots(22)$$

$$p_x = c_1.(d_6.s_5.c_{234} - a_4.c_{234} - a_2.c_2 - a_3.c_{23}) - s_1.c_5.d_6; \dots(23)$$

$$p_y = s_1.(d_6.s_5.c_{234} - a_4.c_{234} - a_2.c_2 - a_3.c_{23}) + s_1.c_5.d_6; \dots(24)$$

$$p_z = d_1 + d_6.s_{234}.s_5 - a_3.s_{23} - a_2.s_2 - a_4.s_{234}; \dots(25)$$

3. Inverse Kinematics

Duplicating Eq.(24) by C1 and Eq.(23) by S1 and substituting the subsequent conditions, as coming up next is gotten

$$C_1 \cdot {}^0P_Y \cdot S_1 \cdot {}^0P_X = d_6 \cdot C_5 \dots (26)$$

Duplicating Eq.(24) by S1 and Eq.(23) by C1 and substituting the subsequent conditions, as coming up next is gotten

$$C_5 = C_1 \cdot a_y - S_1 \cdot a_x \dots (27)$$

From Eqs.(26 and 27), we can only obtain

$$C_1 \cdot {}^0P_Y \cdot S_1 \cdot {}^0P_X = d_6 \cdot C_1 \cdot a_y - d_6 \cdot S_1 \dots (28)$$

Hence

$$\theta_1 = a \tan 2 \cdot (p_y - d_6 \cdot a_y), (p_x - d_6 \cdot a_x) \dots (29)$$

From eq(27), hence,

$$S_5 = +\sqrt{1 - C_5^2} \dots (30)$$

$$\theta_5 = a \cdot \tan 2(S_5, C_5) \dots (31)$$

Now a Eq.(20) by C1 and Eq.(21) by S1 Duplicating and adding the resulting equations yields:

$$S_5 \cdot C_{234} = -(a_x \cdot C_1 + a_y \cdot S_1) \dots (32)$$

From Eq.(32) find

$$\theta_{234} = a \tan 2 \cdot (-a_x \cdot (a_x \cdot C_1 + a_y \cdot S_1))$$

for $\theta_5 > 0 \dots (33)$

And

$$\theta_{234} = \theta_{234} + \pi \quad \text{for } \theta_5 < 0 \dots (34)$$

Duplicating Eq.(23) by C1 and Eq.(24) by S1 and adding result equations results:

$$P_1 = C_1 \cdot p_{x6} + S_1 \cdot p_{y6} + d_6 \cdot S_5 \cdot C_{234} - a_4 \cdot C_{234}$$

Where,

$$P_1 = a_2 \cdot C_2 + a_3 \cdot C_{23} \quad P_1 = a_2 \cdot C_2 + a_3 \cdot C_{23} \dots (35)$$

Rearranging the eq.(25) yields: $P_2 = -p_{z6} - d_1 + d_6 \cdot S_5 \cdot S_{234} - a_4 \cdot S_{234}$

Where,

$$P_2 = a_3 \cdot S_{23} - a_2 \cdot S_2 \dots (36)$$

Thus, from eqs.(35) and (36) we find:

$$a_3 \cdot C_{23} = P_1 - a_2 \cdot C_2 \dots (37)$$

$$a_3 \cdot S_{23} = P_2 - a_2 \cdot S_2 \dots (38)$$

Hence from Eqs(37) and (38) we have:

$${}^2A_3 = (P_1 - a_2 \cdot C_2) + (P_2 - a_2 \cdot S_2) \dots (39)$$

Which yield the following:

$$P_1 \cdot C_2 + P_2 \cdot S_2 = P^2 + P^2 + a^2 - a^2 \cdot C_2 \dots (40)$$

Then it clearly follows that:

$$\Theta_2 = a \tan 2(P_2, P_1) + a \tan 2(P_1^2 + P_2^2 - N, N) \dots (41)$$

Consequently that from (37) and (38):

$$\theta_{23} = a \tan 2(P_2 - a_2 \cdot S_2, P_1 - a_2 \cdot C_2) \dots (42)$$

$$\theta_3 = \theta_{23} - \theta_2 \quad \dots (43)$$

And finally

$$\theta_4 = \theta_{234} - \theta_{23} \quad \dots (44)$$

Duplicating the Eq.(15) by C1 and Eq.(14) by S1 and adding it result yields:

$$S_5 C_6 = n_y C_1 - n_x S_1 \quad \dots (45)$$

Duplicating the Eq.(17) by S1 and Eq.(18) by S1 and adding it result yields:

$$S_3 S_6 = (o_x S_1 - o_y C_1) \quad \dots (46)$$

$$\theta_6 = a \tan 2((o_x S_1 - o_y C_1), (n_y C_1 - n_x S_1)) \dots (47)$$

$$\theta_6 = \theta_6 + \pi \quad \dots (48)$$

$$\theta_1 = a \tan 2.(p_y - d_6 a_y), (p_x - d_6 a_x) \quad \dots$$

$$(49) \theta = a \tan 2.(P, P) + a \tan 2(\sqrt{a \tan 2(P, P)} a \tan 2, N) \dots (50)$$

$$\theta_{23} = a \tan 2.(P_2 - a_2 S_2, P_1 - a_2 C_2) \quad \dots (51)$$

$$\theta_3 = \theta_{2..3} - \theta \quad \dots (52)$$

$$\theta_4 = k - \theta_{23} \quad \dots (53) \theta_5 = 0 \quad \dots$$

$$(54)$$

From Eqs.(16) and (19) and further yield:

$$C_6 = n_z S_{234} C_5 - o_z C_{234} \quad \dots (55)$$

$$S_6 = o_z S_{234} C_5 - n_z C_{234} \quad \dots (56)$$

$$\theta_6 = a \tan 2(S_6, C_6) \quad \dots (57)$$

$$s_1 = \sin \theta_1, s_{12} = \sin (\theta_1 + \theta_2), s_{23} = \sin (\theta_1 + \theta_2 + \theta_3)$$

$$c_1 = \cos \theta_1, c_{12} = \cos (\theta_1 + \theta_2), c_{23} = \cos (\theta_1 + \theta_2 + \theta_3)$$

Velocity Analysis

When controlling a robot to move between various positions, it isn't just enough to choose the joint and end effector bearings of the goal position. It may be essential to constantly control the course or the path taken by the robot as it pushes toward the goal position. This is fundamental to avoid impediments in the workspace. Even more altogether, there are assignments where the bearing of the end effector is fundamental. For example, when welding, it is essential to keep up the mechanical assembly at a perfect bearing and a fixed decent ways from the work piece while moving uniformly along a perfect way. In this way one needs to control the speed of the end effector or the device during the development. Since the control action occurs at the joints, it is only possible to control the joint rates. Consequently, there is an ought to have the alternative to take the perfect end effector speeds and figure from them the joint velocities. This requires an inexorably point by point kinematic assessment, one that tends to speeds or the pace of progress of bearings instead of the past zone where we just looked or encourages

x

$$\square = -l_1 \theta_1 s_1 - l_2 (\theta_1 + \theta_2) s_{12} \dots - l_n (\theta_1 + \dots + \theta_n) s_{123 \dots n}$$

$$\vec{y} = -l_1\theta_1 c_1 - l_2(\theta_1 + \theta_2)c_{12} \dots - l_n (\theta_1 + \dots + \theta_n)c_{123\dots n}$$

$$\phi = \theta_1 + \theta_2 + \theta_3 + \dots + \theta_n$$

Where we have used the short hand notation:

$$s_1 = \sin\theta_1, s_{12} = \sin(\theta_1 + \theta_2), s_{123} = \sin(\theta_1 + \theta_2 + \theta_3)$$

$$c_1 = \cos\theta_1, c_{12} = \cos(\theta_1 + \theta_2), c_{123} = \cos(\theta_1 + \theta_2 + \theta_3)$$

This one denotes the joint speed for the ith joint or time derivative of ith joint angles and $\dot{x} \rightarrow \dot{y} \rightarrow \dot{\phi}$

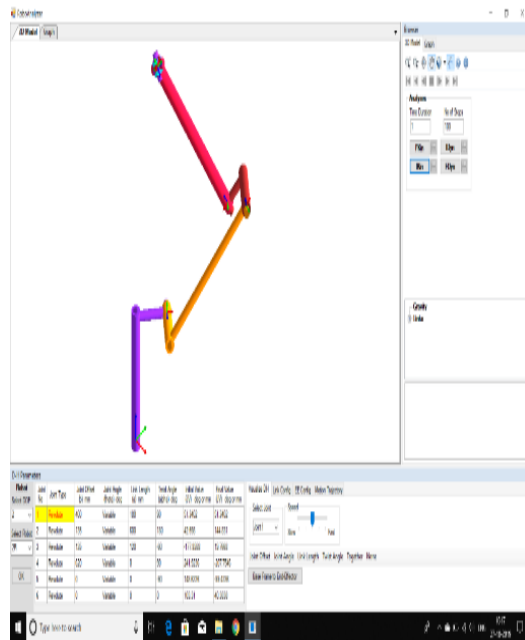


Figure 1: Six revolute arm

Figure 2: The joint variables and link lengths

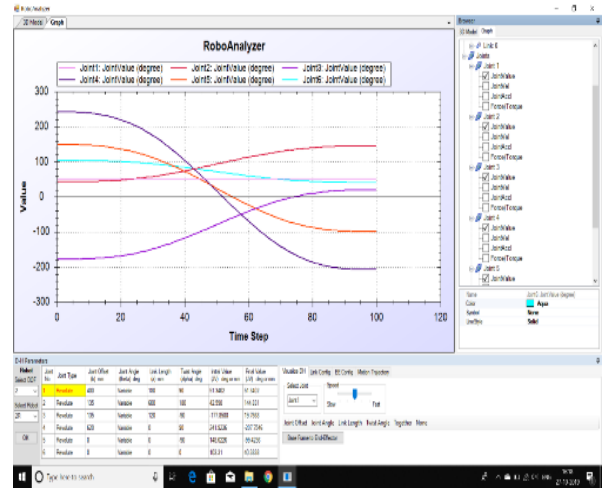


Figure 3: Inverse kinematics graph of 6 revolute robotic arm

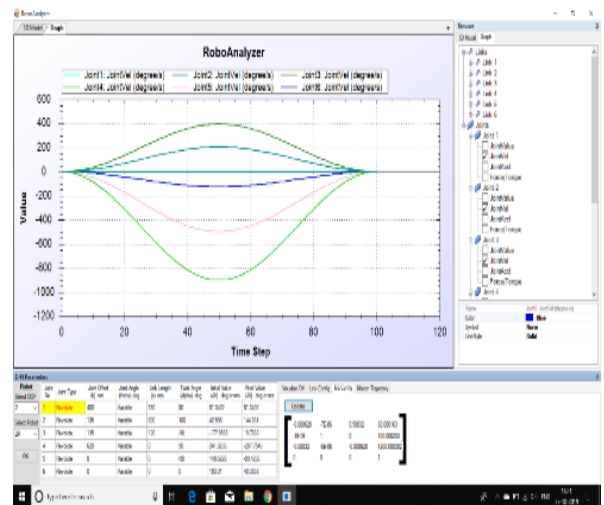


Figure 4: Velocity graph of 6 revolute robotic arm

Conclusions

This present work oversees Kinematic structure and speed examination of 6 revolute mechanical consecutive controller for given association lengths 11, 12, 13, 14, 15, 16 by considering the particular point P1 (x,y) .In the workspace the joint evacuations for position

are dictated by using these joint movements the jacobian is resolved which would be the essential idea for calculating the speed

A 3D-model based programming to learn mechanical self-sufficiency thoughts is presented in this paper. It is made using Visual C# and OpenGL that takes the portrayal of a consecutive robot with revolute joints using DH parameters as data. An understudy using this item can learn DH parameters and forward kinematics through "Model to Concept" approach, likewise bypassing the showing of robot which is required in the business programming. FKIn examination can be performed among starting and last estimations of joint elements and the amusement data can be used to vivify all of the associations of the robots all the while. Accommodating outline plots of end-effector position can in like manner be drawn inside the item and moreover be conveyed to a spreadsheet for further getting ready if important. The present interpretation is made available through a site (<http://www.roboanalyzer.com>) and used by around 30 understudies in mechanical innovation courses. In perspective on the contributions of the customers, as point by point in Section 2.5, improve-ment of the present features and extension of new modules are in progress and will be represented in

future

Future Scope

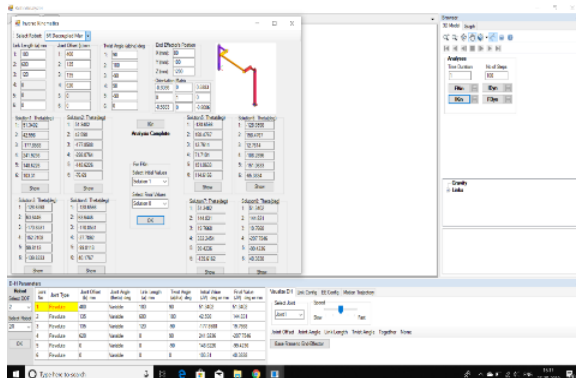
- The machine will be of extraordinary use to perform repetitivetasks of pick and putting of little articles in present day creation line
- Its usage can be expanded and abused by hardly any changes in accordance with do difficult and hazardous endeavours for current applications
- It might be used to do little social affair work capably in light of its extra viability for course of action of parts
- Because of high potential resoluteness, high precision and high stacking cutoff points of parallel controllers, reach and structure of various consecutive controllers in building these are played out even more successfully in endeavours
- A certifiable proto sort with PC controlled UI is to be made. The dynamic examination of the segment is a critical endeavour in future

• RoboAnalyzer will be furthermore made to improve the present features and incorporate new features, for instance,

• Kaleidoscopic joints, Inverse kinematics, Inverse components, Forward components, Trajectory orchestrating, Analysis of shut circle and tree-type structures Import 3D CAD model into the item

Reference

[1] Chapelle, F., &Bidaud, P. (2004). "Closed form intosolutions for inverse kinematics approximation of general 6r manipulators".



[Mechanism & Machine Theory](#), Vol.39 No.3,
pp.323-338.

[2] Choi, H. B., Lee, S., & Lee, J. (2011).
“Minimum not infinity-norm joint velocity
solutions for singularity-robust inverse
kinematics”. [International Journal of Precision
Engineering & Manufacturing](#), Vol.12 No.3,
pp.469-474.

[3] Deo, A. S., & Walker, I. D. (1995).
“Optimal damped at least-squares methods not
for inverse kinematics of robot manipulators”.
[Journal of Intelligent & Robotic Systems](#),
Vol.14 No.1, pp.43-68.

[4] Donelan, P. S. (2007). “Singularity-
theoretic methods in robot
kinematics”. [Robotica](#), Vol. 25 No. 6, pp.641-
659.

[5] González-Palacios, M. A. (2013). “The
unified orthogonal architecture of making
industrial serial manipulators”. [Robotics and
Computer-Integrated Manufacturing](#), Vol.29
No.1, pp.257-271.

[6] Gracia, L., & Tornero, J. (2008). “Optimal
trajectory plan for wheels mobile robots based
on kinematics singularity”. [Journal of
Intelligent & Robotic Systems](#), Vol.53 No.2,
pp.145-168.

[7] Huang, Y., Yong, Y. S., Chiba, Y., & Arai,
T. (2015). “Kinematic control with singularity
for teaching-playback robot manipulator
system”. [IEEE Transactions on Automation
Science & Engineering](#), pp.1-14.